Representation Theorems for indefinite quadratic forms and applications

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In this talk the relation between quadratic forms and operators is considered.

The main question is whether a symmetric sesquilinear form b defines a self-adjoint operator B by $b[x, y] = \langle x, By \rangle$ and whether the operator B allows to reconstruct the form \mathfrak{b} . For bounded or semibounded closed forms, classic results give an affirmative answer to these questions.

Here, we investigate these questions for in general unbounded, non-semibounded forms. As an application, Stokes operators on general domains and indefinite differential operators of the type $\operatorname{div} H$ grad are defined and investigated.

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