Renormalization Group in Statistical Mechanics

Saverio Pascazio, Prague, June 09

A) Introduction to critical phenomena. Critical points and order parameter. Fluctuations. Qualitative description. A simple example: the Ising model. Mean field approach.

B) Models, main ideas and basic concepts. Statistical mechanics. Block Hamiltonians and Kadanoff transformations. Ginzburg-Landau model.

C) Landau theory. Gaussian approximation. $T > T_c$ and $T < T_c$. Correlation length and its temperature dependence.

D) Scaling hypothesis. Scale tranformations. The renormalization group. Definition, philosophy and motivation.

E) Fixed points. Critical exponents. Critical region. Free energy. Relevant, irrelevant and marginal fields. The role of dimension.

Textbooks

S.-K. Ma, Modern theory of critical phenomena, Addison-Wesley, 1982.

M. Le Bellac, "Des phénomènes critiques aux champs de jauge" (Savoirs Actuels, InterEditions/Editions du CNRS, 1990).

Notes and personal calculations, available at http://www.ba.infn.it/~pascazio